## **BOARD OF SCHOOL EDUCATION HARYANA Practice Paper -XI**

(2025-26)

## **Marking Scheme MATHEMATICS**

**CODE: 835** 

⇒ Important Instructions: • All answers provided in the Marking scheme are SUGGESTIVE

• Examiners are requested to accept all possible alternative correct answer(s).

	SECTION – A (1Mark × 20Q)	
Q. No.	EXPECTED ANSWERS	Marks
Question 1.	If $A = \{a, b, c, d, e\}$ and $B = \{d, e, f, g\}$ then $(A - B) \cap (B - A)$ is	
Solution:	(A) Ø	1
Question 2	If $U = \{1,2,3,4,5,6,7,8,9\}$ , $A = \{1,3,5,7,9\}$ , $B = \{2,4,6,8\}$ , then $(A \cup B)'$ is	
Solution:	(B) {}	1
Question 3	$\frac{5\pi}{3}$ in degree measure is :	
Solution:	(B) 300°	1
Question 4.	$a + ib$ form of $i^9 + i^{19}$ is:	
Solution:	(c) $0 + i0$	1
Question 5.	If $\frac{1}{8!} + \frac{1}{9!} = \frac{X}{10!}$ then value of x is:	
Solution:	(A) 100	1
Question 6.	$20^{\text{th}}$ term of the G.P. $\frac{5}{2}$ , $\frac{5}{4}$ , $\frac{5}{8}$ , is:	
Solution:	(B) $\frac{5}{2^{20}}$	1
Question 7.	The value of x for which the numbers $-3/11$ , x, $-11/3$ are in G.P	
Solution:	(B) ±1	1
Question 8.	The derivative of cos (x - a) is:	
Solution:	(C) -sin $(x - a)$	1
Question 9.	If the standard deviation of a data is 5, then its variance is:	
Solution:	(A) 25	1
Question10.	If A and B are two mutually exclusive events then,	
<b>Solution:</b>	$(A) A \cap B = \emptyset$	1
Question11.	Find the number of terms in the expansion of $(2x - 5)^8$ .	
<b>Solution:</b>	8 + 1 = 9	1
Question12.	Find the equation of the circle with centre (-2, 3) and radius 4.	

<b>Solution:</b>	$(x+2)^2 + (y-3)^2 = 16$ or $x^2 + y^2 + 4x - 6y - 3 = 0$	1
Question13.	Write the value of $\lim_{x \to 4} \frac{4x+3}{x-2}$ .	
	$X \to 4 X - 2$	1
Solution:	$\lim_{x \to 4} \frac{4x+3}{x-2} = \frac{4 \cdot (4)+3}{4-2} = \frac{19}{2}$	1
Question14.	If v is the variance and $\sigma$ is the standard deviation, then what is the	
	relation between $v$ and $\sigma$ .	1
Solution:	$v^2 = \sigma$	1
Question 15.	Fill in the blank to make the statement true, $\emptyset' \cap A = \dots$	1
Solution:	$\emptyset' \cap A = U$	1
Question 16.	tan (A - B) is equal to	1
Solution:	$tan (A - B) is equal to$ $tan (A - B) = \frac{tanA - tanB}{1 + tanA.tanB}$	1
Question17.	$n_{C_r} = \frac{n!}{(n-r)!}$ (True/ False)	
Solution:	False	1
Question18.	If a bag has only red balls, the probability of picking a blue ball is 1. (True/ False)	
<b>Solution:</b>	False	1
Question19.	<b>Assertion (A):</b> Let $A = \{1,2\}$ and $B = \{3,4\}$ . Then, number of relations	
	from A to B is 16.	
	<b>Reason (R):</b> If $n(A) = p$ and $n(B) = q$ , then number of relations from	
	A to B is 2 <sup>pq</sup> .	
Solution:	(A) Both Assertion (A) and Reason (R) are true and Reason (R) is the	1
	correct explanation of the Assertion (A)	
Question20.	Assertion (A): The point (3, 0, -5) lies on the XZ plane.	
	<b>Reason(R):</b> The coordinates of a point $P(x, y, z)$ in XZ plane are $(0, 0, z)$ .	4
Solution:	(C) Assertion (A) is true and Reason (R) is false.	1
	$\frac{\text{SECTION} - \text{B} (2\text{Marks} \times 5\text{Q})}{\text{SECTION}}$	
Question21.	List all te subsets of the set $\{-1, 0, 1\}$ .	
Solution:	Let $A = \{-1, 0, 1\}$	
	So, all the subsets of the set A are $\emptyset$ , $\{-1\}$ , $\{0\}$ , $\{1\}$ , $\{-1,0\}$ , $\{0,1\}$ , $\{-1,1\}$ ,	2
	{-1, 0, 1}	
Question22.	Find the multiplicative inverse of $\sqrt{5} + 3i$ .	
Solution:	Multiplicative Inverse of $\sqrt{5} + 3i = \frac{1}{\sqrt{5} + 3i}$	
	V . 2.	
	$\Rightarrow M.I. = \frac{1}{\sqrt{5} + 3i} \times \frac{\sqrt{5} - 3i}{\sqrt{5} - 3i}$	1
	$\Rightarrow \qquad = \frac{\sqrt{5} - 3i}{(\sqrt{5})^2 - (3i)^2}$	
	$\Rightarrow \qquad = \frac{\sqrt{5} - 3i}{5 - 9i^2}$	
	$5-9i^2$	

	$\Rightarrow \qquad = \frac{\sqrt{5} - 3i}{5 + 9} = \frac{\sqrt{5}}{14} - \frac{3i}{14}$	1
OR Question22.	Express $(1-i)^4$ in the form of $a + ib$ .	
Solution:	Given $(1-i)^4$	
	$\Rightarrow = (1-i)^2 \cdot (1-i)^2$	
	$\Rightarrow$ = $(1 + i^2 - 2i).(1 + i^2 - 2i)$	1
	$\Rightarrow = (1-1-2i).(1-1-2i)$	
	$\Rightarrow = (-2i). (-2i)$	
	$\Rightarrow$ = $4i^2$	
	$\Rightarrow$ = -4+i0	1
Question23.	Solve the inequality $\frac{3(x-2)}{5} \le \frac{5(2-x)}{3}$ .	
Solution:	3(y-2) $5(2-y)$	
Solution.	We have $\frac{3(x-2)}{5} \le \frac{5(2-x)}{3}$	
	$\Rightarrow 9(x-2) \le 25(2-x)$	
	$\Rightarrow 9x - 18 \le 50 - 25x$	1
	$\Rightarrow 9x + 25x \le 18 + 50$	
	$\Rightarrow 34x \le 68$	
	$\Rightarrow x \leq 2$	
	$\Rightarrow x \in [2, \propto)$	1
	[-, -, /	
Question24.	Find the 10 <sup>th</sup> term of a G.P. whose 3 <sup>rd</sup> term is 24 and 6 <sup>th</sup> term is 192.	
Solution:	We have, $a_3 = ar^2 = 24$ (1)	
	$\Rightarrow a_6 = ar^5 = 192 \qquad \dots (2)$	$\frac{1}{2}$
	Dividing (2) by (1), we have	2
	$\Rightarrow$ $r^3 = 8$	4
	$\Rightarrow$ r = 2	$\left  \frac{1}{2} \right $
	$\Rightarrow a(2)^2 = 24$	
	$\Rightarrow a = 6$	$\frac{1}{2}$
	$\therefore a_{10} = a.r^9 = 6.(2)^9$	
	$a_{12} = 6. (512) = 3072$	$\frac{1}{2}$
Question25.	Find the equation of the parabola with vertex at $(0,0)$ and focus at $(0,2)$ .	2
Solution:	Since the vertex is at $(0,0)$ and the focus is at $(0,2)$ which lies on y-axis.	
	⇒ Y-axis is the axis of the parabola.	

	⇒ Equation of the parabola is of the form $x^2 = 4ay$ ⇒ $a = 2$	1	
	$\Rightarrow x^2 = 4(2)y$ $\Rightarrow x^2 = 8y$	$\begin{bmatrix} \frac{1}{2} \\ \frac{1}{2} \\ \frac{1}{2} \end{bmatrix}$	
	$\Rightarrow x - 6y$	$\frac{1}{2}$	$\frac{1}{2}$
OR Question25.	Find the equation of the ellipse, whose vertices are $(0, \pm 13)$ and foci are $(0, \pm 5)$ .		2
Solution:	Since the vertices are on y-axis, the major axis is along the y-axis.		
	So equation of ellipse is of the form $\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1$		
	Given that $a = \text{semi major axis} = 13$ , and $c = \pm 5$ from foci $(0, \pm 5)$	1	
	And the relation $c^2 = a^2 - b^2$ , gives $5^2 = 13^2 - b^2$ i.e. $b^2 = 144$		
	Therefore, the equation of the ellipse is $\frac{x^2}{25} + \frac{y^2}{144} = 1$	1	
	SECTION – C (3Marks $\times$ 6Q)		
Question26.	If $U = \{1,2,3,4,5,6,7,8,9\}$ , $A = \{2,4,6,8\}$ and $B = \{2,3,5,7\}$ . Verify that $(A \cup B)' = A' \cap B'$ .		
Solution:	Here $A \cup B = \{2,3,4,5,6,7,8\}$		$\frac{1}{2}$
	$\therefore  (A \cup B)' = \{1,9\}$ Now	1	
		1	
	$\therefore A' \cap B' = \{1,9\}$		1
	$\Rightarrow (A \cup B)' = A' \cap B'$		2
Question27.	Find the domain and Range of the function $\sqrt{4-x^2}$ .		
Solution:	Here $y = \sqrt{4 - x^2}$		
	<del>_</del>		
	$\Rightarrow -2 \le x \le 2  \Rightarrow x \in [-2, 2]$		
	Domain = [-2, 2]	$1\frac{1}{2}$	
	Also, $y^2 = 4 - x^2$		
	$\Rightarrow x^2 = 4 - y^2$		
	¥ ·		
	$\Rightarrow (y-2)(y+2) \le 0$ \Rightarrow -2 \le y \le 2 \Rightarrow y \varepsilon [-2, 2]		
Question27. Solution:	Find the domain and Range of the function $\sqrt{4-x^2}$ .  Here $y = \sqrt{4-x^2}$ y will have real values if $4-x^2 \ge 0$ $\Rightarrow x^2 - 4 \le 0$ $\Rightarrow (x-2)(x+2) \le 0$ $\Rightarrow -2 \le x \le 2 \Rightarrow x \in [-2,2]$ Domain = $[-2,2]$ Also, $y^2 = 4 - x^2$ $\Rightarrow x^2 = 4 - y^2$ $\Rightarrow x = \pm \sqrt{4-y^2}$ Clearly x is defined when $4 - y^2 \ge 0$ i.e., when $y^2 - 4 \le 0$ $\Rightarrow (y-2)(y+2) \le 0$		1/2

	But $y = \sqrt{4 - x^2} \ge 0$ for all $x \in [-2, 2]$ i.e., y attains only non-	
	negative values.	
	∴ $y \in [0, 2]$ for all $x \in [-2, 2]$	$1\frac{1}{2}$
	$\therefore \text{Range} = [0, 2].$	2
Question28.	Expand: $\left(x^2 + \frac{3}{x}\right)^4$ ; $x \neq 0$	
Solution:	$\left(x^{2} + \frac{3}{x}\right)^{4} = {}^{4}C_{0}\left(x^{2}\right)^{4}\left(\frac{3}{x}\right)^{0} + {}^{4}C_{1}\left(x^{2}\right)^{3}\left(\frac{3}{x}\right)^{1} + {}^{4}C_{2}\left(x^{2}\right)^{2}\left(\frac{3}{x}\right)^{2} + {}^{4}C_{3}$	
	$\left(x^{2}\right)^{1} \left(\frac{3}{x}\right)^{3} + {}^{4}C_{4} \left(x^{2}\right)^{0} \left(\frac{3}{x}\right)^{4}$	$1\frac{1}{2}$
	$= x^{8} + 4.(x^{6})\left(\frac{3}{x}\right) + 6.(x^{4})\left(\frac{9}{x^{2}}\right) + 4.(x^{2})\left(\frac{27}{x^{3}}\right) + 1.(1)\left(\frac{81}{x^{4}}\right)$	1
	$= x^8 + 12x^5 + 54x^2 + \frac{108}{x} + \frac{81}{x^4}$	$1\frac{1}{2}$
OR Question28.	$= x^{8} + 12x^{5} + 54 x^{2} + \frac{108}{x} + \frac{81}{x^{4}}$ Which is larger $(1.01)^{1000000}$ or $10,000$ ?	
Solution:	$(1.01)^{1000000} = (1 + .01)^{1000000}$	1
		$\frac{1}{2}$
	$= {}^{1000000}$ C <sub>0</sub> (1) ${}^{1000000}$ (.01) ${}^{0}$ + ${}^{1000000}$ C <sub>1</sub> (.01) ${}^{1}$ + other positive terms	.1
	$= 1 + 100000 \times .01 + $ other positive terms	$1\frac{1}{2}$
	= 1 + 10000 +  other positive terms	
	= 10001 + other positive terms	
	>10000	
	Hence $(1.01)^{1000000} > 10000$	1
Question29.	Find the sum of the sequence 8, 88, 888, 888, to n terms.	
Solution:	This is not a GP., however, we can relate it to a GP. by writing the	
	terms as $S_n = 8 + 88 + 888 + 888 +$ to n terms	
	$=\frac{8}{9}[9+99+999+9999+$ to n term]	1
	$= \frac{8}{9} [ (10^{1} - 1) + (10^{2} - 1) + (10^{3} - 1) + (10^{4} - 1) +n \text{ terms} ]$	
	$=\frac{8}{9}[(10+10^2+10^3+n \text{ terms}) - (1+1+1+n \text{ terms})]$	1
	It is a G.P. where $a = 10$ and $r = 10 > 1$	
	$\therefore S_n = \frac{a(r^n - 1)}{r}$	
	$ = \frac{8}{9} \left[ \frac{10(10^{n} - 1)}{10 - 1} - n \right] = \frac{8}{9} \left[ \frac{10(10^{n} - 1)}{9} - n \right] $	1
OR	If A.M. and G.M. of two positive number a and b are 10 and 8	
Question 29	respectively, find the numbers.	
Solution:	Given that A.M. = $\frac{a+b}{2}$ = 10 and G.M. = $\sqrt{a.b}$ = 8	
	$\Rightarrow a + b = 20$ (1) and $ab = 64$ (2)	1_
	Using the identity, $(a - b)^2 = (a + b)^2 - 4ab$ and putting the	2
	respective values, we have	
	$(a-b)^2 = (20)^2 - 4(64)$	

		1
	$a - b = \sqrt{400 - 256}$	1
	$a - b = \pm 12 \qquad \dots (3)$	
	Solving (1) and (3), we obtain	
	a = 4 and $b = 16$ or $a = 16$ and $b = 4$	$1\frac{1}{2}$
	thus the number are 4, 16 or 16, 4 respectively	2
Question30.	Find the equation of the set of the points P such that $PA^2 + PB^2 = 2k^2$ ,	
	where A and B are the points (3, 4, 5) and (-1, 3, -7), respectively.	
Solution:	Let the coordinate of the point P be (x, y, z).	
	$\therefore$ PA = $\sqrt{(x-3)^2 + (y-4)^2 + (z-5)^2}$	
	$\Rightarrow PA^2 = (x-3)^2 + (y-4)^2 + (z-5)^2$	
	Now PB = $\sqrt{(x+1)^2 + (y-3)^2 + (z+7)^2}$	
	$\Rightarrow PB^2 = (x+1)^2 + (y-3)^2 + (z+7)^2$	$1\frac{1}{2}$
	By the given condition $PA^2 + PB^2 = 2k^2$ , we have	
	$(x-3)^2 + (y-4)^2 + (z-5)^2 + (x-3)^2 + (y-4)^2 + (z-5)^2 = 2k^2$	
	$2x^{2} + 2y^{2} + 2z^{2} - 4x - 14y + 4z = 2k^{2} - 109$	$1\frac{1}{2}$
		2
Question31.	In how many ways can a student choose a programme of 5 courses if 9	
	courses are available and 2 specific courses are compulsory for every	
	student?	
Solution:	There are 9 courses available and 5 courses are to be chosen out of 9.	
	Since 2 courses are compulsory for every student.	
	Therefore, now we have to choose 3 courses out of remaining 7 courses.	
	This can be done in <sup>7</sup> C <sub>3</sub> ways	$1\frac{1}{2}$
		2
	$\therefore {}^{7}C_{3} = \frac{7!}{(7-3)! \cdot 3!}$ $= \frac{7 \cdot 6 \cdot 5 \cdot 4}{4 \cdot 3 \cdot 2 \cdot 1} = 35 \text{ ways}$	
	(7-3)!.3! $7.6.5.4$	.1
	$=\frac{1}{4.3.2.1}$ = 35 ways	$1\frac{1}{2}$
	SECTION – D (5Marks × 4Q)	
Ougstion 22	` '	
Question32.	(i) Prove that: $\frac{\sin 5x - 2\sin 3x + \sin x}{2} = \tan x$	
	$\cos 5x - \cos x$	
	(ii) Prove that: $\cot^2 \frac{\pi}{6} + \csc \frac{5\pi}{6} + 3 \tan^2 \frac{\pi}{6} = 6$	
Solution: (i)	$\frac{\sin 5x - 2\sin 3x + \sin x}{\sin 5x} = \tan x$	
	$\cos 5x - \cos x$	
	$\sin 5x + \sin x - 2\sin 3x$	
	$L.H.S. = {\cos 5x - \cos x}$ [rearranging]	

	Using $\cos C - \cos D = 2\sin\left(\frac{C+D}{2}\right).\sin\left(\frac{C-D}{2}\right)$		$\frac{1}{2}$
	and $\sin C + \sin D = 2\sin(\frac{C+D}{2}).\cos(\frac{C-D}{2})$ , we have		2
	$\Rightarrow = \frac{2\sin 3x \cdot \cos 2x - 2\sin 3x}{2\sin 3x}$	1	
	$-2\sin 3x \cdot \sin 2x$	1	
	$\Rightarrow = \frac{2\sin 3x \cdot (\cos 2x - 1)}{-2\sin 3x \cdot \sin 2x}$	$\frac{1}{2}$	
	$\Rightarrow = \frac{1 - \cos 2x}{\sin 2x}$		
	$\Rightarrow = \frac{2\sin^2 x}{2.\sin x .\cos x}$		
	$\frac{1}{2 \cdot \sin x \cdot \cos x}$	1	
	$\Rightarrow = \tan x$		
	$\Rightarrow$ L.H.S. = R. H.S.		
Solution:(ii)	2 П 2 П		
	L.H.S. = $\cot^2 \frac{\pi}{6} + \csc \frac{5\pi}{6} + 3 \tan^2 \frac{\pi}{6}$		
	$=> (\cot \frac{\pi}{6})^2 + \csc (\pi - \frac{\pi}{6}) + 3 (\tan \frac{\pi}{6})^2$		
	We have,	1	
	$= (\sqrt{3})^2 + \csc \frac{\pi}{6} + 3(\frac{1}{\sqrt{3}})^2$	1	
	$= 3 + 2 + 3 \cdot \frac{1}{3}$		
	= 3+2+1=6	1	
	$\Rightarrow$ L.H.S. = R. H.S.		
Question33.	Find the coordinates of the foot of perpendicular from the point (-1, 3)		
	to the line $3x - 4y - 16 = 0$ .		
Solution:	Given equation of line $3x - 4y - 16 = 0$ (1)		
	Let the foot of perpendicular be $(x, y)$ from $(-1, 3)$ . Since line joining $(x, y)$ and $(-1, 3)$ and the given line $3x - 4y - 16 = 0$		
	are perpendicular with each other		
	:. Equation of any line perpendicular to $3x - 4y - 16 = 0$ is		
	4x + 3y + k = 0	1	
	Now line (2) is passing through (-1, 3) $\Rightarrow$ 4(-1) + 3(3) + k = 0		
	$\Rightarrow k = -5$		
	:. Equation of line passing through (-1, 3) and $\perp$ ar to $3x - 4y - 16 = 0$ is	$1\frac{1}{2}$	
	$4x + 3y - 5 = 0 \qquad(3)$	2	
	Now solving equations (1) and (3)(any method), we obtain $3x - 4y = 16$ (4)		
	4x + 3y = 5		
	Multiply (4) by 3, (5) by 4 and then adding, we have		

		1
	$25x = 68 \implies x = \frac{68}{25}$ using this value in (5), we have	
	$4\left(\frac{68}{25}\right) + 3y = 5 \implies 3y = 5 - \frac{272}{25}$ $3y = \frac{125 - 272}{25} \implies 3y = \frac{-147}{25}$	
	$3v = \frac{125 - 272}{3v} \implies 3v = \frac{-147}{3v}$	
	$y = \frac{25}{25}$ 25	
	23	$2\frac{1}{2}$
	So foot of perpendicular is $(\frac{68}{25}, \frac{-49}{25})$	2
OR	Find the equation of the lines through the point (3, 2) which make an	
Question33.	angle of 45° with the line $x - 2y = 3$ .	
Solution:	Given equation of line $x - 2y = 3$ and $\theta = 45^{\circ}$	
	$\therefore \text{Slope of line} = \frac{-\text{coeff.of x}}{\text{coeff.of y}} = \frac{-1}{-2} = \frac{1}{2}$	
	$m_1 = \frac{1}{2}$	1
	Let m be the slope of required line.	<u>2</u>
	Now tan $\theta = \left  \frac{m_1 - m_2}{1 + m_1 \cdot m_2} \right ^2$	1
		2
	$\Rightarrow \tan 45^\circ = \left  \frac{m_1 - \frac{1}{2}}{1 + m_1 \cdot (\frac{1}{2})} \right $	
	$\Rightarrow 1 = \left  \frac{m_1 - \frac{1}{2}}{1 + \frac{m_1}{2}} \right $	
	$\Rightarrow \pm 1 = \frac{m_1 - \frac{1}{2}}{1 + \frac{m_1}{2}}$	
	$\Rightarrow 1 + \frac{m_1}{2} = m_1 - \frac{1}{2}$ or $-1 - \frac{m_1}{2} = m_1 - \frac{1}{2}$	
	$\Rightarrow \frac{-m_1}{2} = \frac{-3}{2}  \text{or}  \frac{3m_1}{2} = \frac{-1}{2}$ $\Rightarrow m_1 = 3  \text{or}  m_1 = \frac{-1}{3}$	
	$\Rightarrow$ m <sub>1</sub> = 3 or m <sub>1</sub> = $\frac{-1}{2}$	2
	∴ Equations of lines through (3, 2) having slopes 3 and -1 are	
	$y-2=3(x-3) \implies 3x-y=7$	
	and $y-2=\frac{-1}{3}(x-3) \implies x+3y=9$	2
Question34.	Find the derivative of cos x from first principle.	
Solution:	Let $f(x) = \cos x$ , the	
	$\frac{d(f(x))}{dx} = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$	
	$ \begin{vmatrix} dx & h \to 0 & h \\ 1 & \cos(x+h) - \cos(x) \end{vmatrix} $	
	$= \lim_{h \to 0} \frac{\cos(x+h) - \cos(x)}{h}$	1
	$= \lim_{h \to 0} \left[ \frac{-2\sin(\frac{x+h+x}{2})\sin(\frac{x+h-x}{2})}{h} \right] \qquad \text{[using cos C - cos D = -2 sin(\frac{C+D}{2}).sin(\frac{C-D}{2})]}$	2
	$= -\lim_{h \to 0} \left[ \frac{\sin(\frac{2x+h}{2})\sin(\frac{h}{2})}{\frac{h}{2}} \right]$	
	$h \rightarrow 0$ $\left[ \frac{n}{2} \right]$	

	[.:/h.]	
	$= -\lim_{h \to 0} \left[ \sin\left(\frac{2x+h}{2}\right) \right] \cdot \lim_{h \to 0} \left[\frac{\sin\left(\frac{h}{2}\right)}{\frac{h}{2}}\right]$	2
OD	$= -\sin x \cdot (1) = -\sin x$	
OR Question34.	$\left(mx^2 + n,  x < 0\right)$	
2	Suppose $f(x) = \begin{cases} nx + m, & 0 \le x \le 1 \text{ . For what value of m and n} \\ nx^3 + m, & x > 1 \end{cases}$	
	does both $\lim_{x\to 0} f(x)$ and $\lim_{x\to 1} f(x)$ exists?	
Solution:	Here, limit exist at $x \to 0$	
	i.e., $LHL = RHL$ (1)	
	LHL at $x \to 0$	
	$= \lim_{x \to 0-} f(x)$	
	$= \lim_{h \to 0} f(0 - h)$	
	$= \lim_{h \to 0} [m(-h)^2 + n]$	
	$= n \qquad \dots (2)$	$1\frac{1}{2}$
	RHL at $x \rightarrow 0$	1 2
	$= \lim_{x \to 0+} f(x)$	
	$x\rightarrow 0+$ $-\lim_{n\to\infty} f(0 \perp h)$	
	$= \lim_{h \to 0} f(0+h)$	
	$= \lim_{h \to 0} [n(0+h) + m]$	
	$= m \qquad \dots (3)$	<sub>1</sub> 1
	From (1), (2) and (3)	$1\frac{1}{2}$
	n = m	
	Here, limit exist at $x \rightarrow 1$	
	i.e., $LHL = RHL$ (1)	
	LHL at $x \rightarrow 1$	
	$= \lim_{x \to 1^-} f(x)$	
	$= \lim_{h \to 0}^{x \to 1-} f(1-h)$	
	$h \rightarrow 0$ - $\lim [n(1-h) + m]$	
	$= \lim_{h \to 0} [n(1-h) + m] $	
	$= n + m \qquad \dots (2)$	1
	RHL at $x \rightarrow 1$	1
	$= \lim_{x \to 1+} f(x)$	
	$= \lim_{h \to 0} f(1+h)$	
	$= \lim_{h \to 0} [n(1+h)^3 + m]$	
	$= n + m \qquad \dots (3)$	
	For $\lim_{x \to \infty} f(x)$ to exists, we need $n = m$	
	For $\lim_{x\to 0} f(x)$ exists for any integral value of m and n.	1
	$x \to 1$	
	I.	L

Question35.	Calarilata					Co., 410 o Fo.11.		<del></del>
Question33.	Calculate medistribution.		e and standa	ra aevi	auon 1	or the lone	owing	
	Classes		-20 20-30	30-40	40-50			
	Frequency	5	8 15	16	6			
	Trequency							
Solution:								
	From the give	ven data, we	construct th	e follov	ving ta	able.		
	Class	Емодионом	Midpoint	f <sub>i</sub> x		(v. <del>v.</del> )2	<b>f</b> (** = 7)2	
	Class	Frequency f <sub>i</sub>	Xi	113	41	$(\mathbf{x}_{i} - \bar{\mathbf{x}})^{2}$	$\int f_i(x_i - \bar{x})^2$	
	0 – 10	5	5	25	5	484	2420	
	10 - 20	8	15	12		144	1152	
	20 - 30	15	25	37		4	60	
	30-40	16	35	56		64	1024	
	40 - 50	50	45	125		324	1944	
		50		135	00		6600	
	T1	M	$=$ $ ^{1}$ $\nabla i$ $=$ $^{7}$	£				
	Thus	Mean	$\bar{\mathbf{x}} = \frac{1}{N} \sum_{i=1}^{i=7}$	$J_i x_i$				
			$=\frac{1350}{50}=$	27				$3\frac{1}{2}$
	Variance ( o	$(2) = \frac{1}{2} \sum_{i=1}^{i=1}$	$\frac{7}{7} f_{\cdot} (\gamma_{\cdot} - \bar{\gamma}_{\cdot})$	<del>-</del> )2				
	variance ( 0	$N^{\Delta i}=$						
			$=\frac{6600}{50}=$	132				1
	and Stand	dard deviation	$on(\sigma) = \sqrt{13}$	$\overline{2} = 11$	.49			1
		SEC	TION – E	(4Marl	zs × 3	<u>()</u>		2
Question36.	The sum or			-		-	sformed	
Zarstiviisu.	into a produ		_					
	formulae:					, 10110 W	<del></del> 5	
		$+\sin D = 2$	$\sin \frac{C+D}{2} \cos$	C-D				
			$\cos \frac{c^2 + D}{2} \sin \frac{c}{2}$					
	(0) 3111 (	- sm D - 2	C+D = SIII	2 C-D				
	(c) cos C	$C + \cos D = 2$	$2\cos\frac{C+D}{2}\cos\frac{C}{2}$	$s \frac{1}{2}$				

	(d) $\sin C + \sin D = 2 \sin \frac{C+D}{2} \sin \frac{D-C}{2}$							
	Based on the above information, answer the following questions.							
	(i) The value of sin 80° - sin 20° is: (a) cos 30° (b) cos 60° (c) sin 30° (d) cos 50° (1) (ii) The value of cos 15° - sin 15° is:							
	(a) $\frac{1}{\sqrt{2}}$ (b) $\frac{\sqrt{3}}{2}$ (c) $\frac{1}{2}$ (d) $\frac{-1}{\sqrt{2}}$ (1)							
	(iii) sin 70° + sin 80° is equal to: (a) 2 cos15°.cos 5°(b) 2 sin15°.sin 5°(c) 2 cos15°.sin 5°(d) None of these (1)							
	(iv) $\sin 51^{\circ} + \cos 81^{\circ} - \cos 21^{\circ}$ is equal to: (a) 1 (b) 0 (c) -1 (d) 2 (1)							
Solution:	(i) (d) cos 50°	1						
	$(ii)  (a) \ \frac{1}{\sqrt{2}}$	1						
	(iii) (a) 2 cos15°.cos 5°	1						
	(iv) (b) 0	1						
Question37.	In a class of 60 students, 30 opted for NCC, 32 opted for NSS and 24 opted for both NCC and NSS. One of the students is selected at random from the class.  Based on the above information answer the following questions:							
	(i) The probability that the student has opted for only NCC is: $(a)\frac{1}{2} \qquad (b)\frac{1}{10} \qquad (c)\frac{19}{30} \qquad (d)\frac{11}{30}$ (ii) The probability that the student has opted for both NCC and NSS is: $(a)\frac{1}{2} \qquad (b)\frac{2}{5} \qquad (c)\frac{19}{30} \qquad (d)\frac{11}{30}$ (iii) The probability that the student has opted for NCC or NSS is: $(a)\frac{1}{2} \qquad (b)\frac{2}{5} \qquad (c)\frac{19}{30} \qquad (d)\frac{2}{15}$ (iv) The probability that the student has opted neither both NCC nor NSS is: $(a)\frac{1}{2} \qquad (b)\frac{2}{5} \qquad (c)\frac{11}{30} \qquad (d)\frac{2}{15}$							
Solution:	(i) (b) $\frac{1}{10}$	1						
	(ii) (b) $\frac{2}{5}$ (iii) (c) $\frac{19}{30}$	1						
	$(iii)$ $(c)\frac{19}{30}$	1						
	(iv) (c) $\frac{11}{30}$	1						

Question	Indian track and field athlete Neeraj Chopra, who completes in the	
38.	javelin throw, won a gold medal at Tokyo Olympics. He is the first	
	track and field athlete to win a gold medal for India at the Olympics.	
	Based on above information, answer the following:	
	(i) Name the shape of paths followed by javelin. (1)	
	(ii) If the equation of such curve is given by $x^2 = -16y$ , then write coordinate of foci. (1)	
	(iii) Write the equation of directrix and length of semi- latus rectum. (2)	
Solution: (i)	Shape of path is Parabola.	1
(ii)	Comparing $x^2 = -16y$ with standard form $x^2 = -4ay$ we have	
	$\Rightarrow$ $-4a = -16$	
	$\Rightarrow$ a = 4	
	:. <b>Focus:</b> $(0,-a) = (0,-4)$	1
(iii)	Equatio of Directrix:	
	y = a	
	$\Rightarrow$ $y = 4$	
	Length of latus rectum:	2
	$4 a = 4 \times 4 = 16$	_